A Novel Nonlinear Optimization Coverage Algorithm in Wireless Sensor Networks

Huiling Peng, Zeyu Sun* and Yuanbo Li

School of Computer and Information Engineering, Luoyang Institute of Science and Technology, Luoyang 471023, China.
E-mail:lylgszy@163.com

Abstract

Maximize coverage and prolong the network lifetime for wireless sensor networks has become one of the key topics of research. For this, put forward a kind of node scheduling strategy based on covering algorithm. The algorithm by Poisson distribution model structure node density formula, according to the node density formula in the monitoring region deploying to effective coverage; On the other hand, through the node state scheduling mechanism updates as well as to the neighbor node, can be made of residual energy of nodes and monitoring the area sensor the node energy consumption balance, so as to prolong the network lifetime goal. The simulation results show that, the algorithm can not only useless nodes completely too effective coverage, improve the coverage while optimizing the cyber source configuration, prolong the network lifetime.

Keywords: wireless sensor network; network lifetime; coverage rate; sensor nodes

1. Introduction

Wireless sensor network with other network there are certain differences in the architecture. Firstly, in terms of the wireless sensor network itself, and it is through the dense nodes of monitoring area control, sensor nodes are smaller and energy[1], LTD; In some of the more severe and dangerous environment, the energy of the sensor nodes and can't effectively supplement; Second, in the high-density deployment of monitoring area, when in the working state of multiple sensor nodes to a particular target monitoring, location, coverage and tracking, will lead to multiple data collected by the sensor node or calculated information to a neighbor node and generated when the base station sends a large number of redundant data, it will inevitably cause the network congestion, leading to a large number of useless sensor node energy consumption, will eventually lead to the total energy of the wireless sensor network (WSN) too quickly consumption, reduces the amount of effective network life cycle. Thirdly, in the process of practical application, not all of the target node should be completely covered. That a node is the focus on target node, which begs to effectively cover completely cover or K degree, that is, the destination node in a sensor node K perceived scope. When the destination node is not concern, let their perception in a sensor node scope. In the process of cover, still need to consider in a certain conditions, some sensor nodes in a dormant state, in order to effectively guarantee the network energy, prolong the network life cycle.

Therefore, how to fulfill the coverage and connection of designated regions and suppress the excessive energy consumption of sensor nodes at the least sensor nodes under the condition of certain coverage is a challenge. Based on the above ideas, three issues should be solved. Firstly, planning the monitored target node to a square region, the association model between the sensor node and destination node is established to place the target node within the range of the sensor nodes. Secondly, by using of the mobile node scheduling strategy and parameters dynamically change, coverage region of mobile node is reduced, which achieves effective coverage of the target region, and enhance the
network topology. Thirdly, the number of the minimal sensor nodes should be obtained by using the probability expectations under the conditions of required coverage. Under the premise of ensuring the balance of scheduling node and meeting the quality of network coverage, connectivity probability model, non-boundary coverage and node variation curve is given, considering the actual situation of edge nodes. By calculating and reasoning of the side length of covering region, the number of nodes required under the different rates of coverage and connectivity.

2. Related Works

In recent years, many domestic and foreign experts and scholars put forward many theories and solutions on the coverage of wireless sensor networks and connectivity issues. The idea proposed by [2] to study the sensor coverage and restore connectivity of mobile nodes is to study coverage and connectivity as a whole, and by restoring one or more invalid neighbor node by using the algorithm of sensor coverage and restore connectivity to reposition each neighbor node and replace the invalid nodes to restore to the initial position, thereby forming a recovery connectivity and monitoring all the target nodes in the initial position of the coverage region. In the Boolean 0/1 perceptual model given by [3] gives, the probability of occurrence of events within the perception radius is defined as 1 and the probability of events outside the perception radius defined as 0. But in the actual application process, the perception of the sensor nodes is apparent gradually decreasing, and their perceptions will gradually decreasing to zero when the number of dead nodes exceeds a certain number. The Co-Grid algorithm given by [4] is to divide the target region into boundary overlapping regions, and to select the configuration mode of minimal nodes number in each unit by prediction of the perceived probability model. To a large extent, the above algorithms can complete the coverage and connectivity, but the solution processes are far too complex. In addition, with the increase of the sensor nodes and coverage region changes, the complexity of the algorithm will become larger, and thus computational efficiency will reduces. The density control algorithm PEAS given by [5] uses each of dormant sensors to detect the state of its neighbor nodes within its coverage region, which is that the node will get into working condition if there is no working node in the coverage region; otherwise it will fall into dormant state.

It is obvious that the PEAS algorithm can easily lead to the fast death of some nodes, and uneven node energy consumption. The algorithm given by [6] to cover the convex region of the active node set, the node's communication radius is greater than or equal to twice the sensing radius, in order to ensure full connectivity sufficient condition. The coverage configuration protocol (CCP) proposed by [7] is to judge the distributive node functions qualification using the local node location information, which is when the communication radius is greater than or equal to 2 times the sensing radius and the network k-cover the given convex region in the region, the network is k-connected, thereby promoting its agreement to meet the multi-coverage requirements. LEACH protocol has been improved in reference [8]. The main idea is: clustering routing algorithm uses periodic random selection of cluster head node to balance the node energy consumption and to achieve the purpose to extend the network lifetime.

All of the above algorithm is to a large extent can be completed the coverage and connectivity, but the solving process is too complex; in addition, with the increase of the number of sensor nodes and coverage area change [9-11], also can make the algorithm complexity is increased, thereby reducing the computational efficiency [12-13]. The above six algorithms in different degree to satisfy a condition coverage requirements, but also can guarantee the connectivity of the network, but its disadvantage is node distribution unevenness caused the complexity of the algorithm is too high, speed too slow, and a plurality of sensor node position changes will occur more frequently perceived area multiple cover the possibility[13-15].
3. Model Analysis

3.1. Basic Hypothesis

The following hypotheses are advanced on the network model:

Hypothesis 1: the monitored area is much larger than the sensor node sensing area, not considering the boundary factors on the monitoring of regional influence.

Hypothesis 2: sensor node sensing radius and radius of communication will appear a disk shape and the communication radius greater than or equal to 2 times the radius of perception.

Hypothesis 3: each sensor node can be through their own information to their location information.

Hypothesis 4: the initial state, and each sensor of node energy is the same, all sensor nodes have the same processing capacity, and equal status [16].

3.2. Basic Definition

Definition 1: the distance between any two nodes \( d(i,j) \) are called nodes \( i \) and \( j \) Euclidean distance, when \( d(i,j)<2R \) referred to the neighbor node, node \( i \) and \( j \).

Definition 2: in the monitoring of the target area, when a target node is \( K \) sensor node coverage, called \( K \) heavy cover.

Definition 3: in the monitoring of the target area, all sensor nodes coverage Union and all sensor nodes range and then, called network covering efficiency:

\[
EA = \frac{\bigcup S_i}{\sum S_j}
\]  

Definition 4: Covering the region of coverage for:

\[
P(s_i,s_j)=e^{-d^2}
\]

Among them is sensor node physical parameters; \( R \) said sensor node monitoring dynamic parameters in the said sensor nodes; \( d(s_i,s_j) \) Euclidean distance; when \( d(s_i,s_j)\leq(R_s-R_e) \), this time node \( S_i \) is detected, it is not detected.

Definition 5: suppose that nodes \( s_i, s_j \), the target regions they cover are \( C_i \) and \( C_j \), and \( C_i \cap C_j\neq\emptyset \), so nodes \( s_i \) and \( s_j \) are coverage connected. Suppose that \( T \) is a m nodes set randomly distributed in the target region, \( E \) is the set of edges of the network diagram, indicating that the \( e_{ij}=1 \) positional relationship in \( e_{ij} \); \( e_{ij} \) represents the positional relationship of node \( s_i \) and the target node \( t_j \). When \( e_{ij}=1 \) when and only when the Euclidean distance of target node \( t_j \) and the node \( s_i \) is less than or equal to the perception radius \( r_i \), otherwise \( e_{ij}=0 \). \( W=[w_1,w_2,w_3,…w_n] \) is the initial energy set of sensor nodes; \( W \) is in normal distribution; the \( w_i \) represents initial energy of sensor node \( s_i \); \( w_i \) is the maximum energy in the process of node work.

Theorem 1: when and only when the three equal circles intersect at one point, and form an equilateral triangle length of a side is 1.732, covering the efficiency of \( EA \) maximum, that is: \( EA \leq 82.73\% \)

Proof: As shown in figure1:

![Figure 1. Intersection of Two Circles](image-url)
Firstly, figure 1 was analyzed, as are three. Two intersect, and the intersection region is equal, so $\Delta O_1O_2O_3$ is an equilateral triangle, with side length $O_1O_2$ is $r$, an equilateral triangle $\Delta O_1O_2O_3$ three interior angles are respectively $\pi/3$, $\angle O_1O_2O_3=\pi/3$, $S_{\Delta O_1O_2O_3}=0.5r^2\sin\pi/3$, since three, round two intersection, and completely covered on the plane the Euclidean distance, $d_1<2r$, let the equilateral triangle $\Delta O_1O_2O_3$, the maximum length to keep the $S_{\Delta O_1O_2O_3}$ area is the largest, the three circle intersect at a point, as shown in Figure 1 as shown, connect to the and extended to two points to, connecting the, set three the radius of the circle of 1, $S_{\Delta O_1O_2O_3}=0.433$, according to the formula (1) we get $EA=82.73\%$.

Theorem 2: sensor node monitoring area $A$, the monitoring of regional node density, a monitoring area $A$ node number $X$ subject to node $K$ probability density:

$$P(X=k)=e^{-\lambda A}\frac{(\lambda A)^k}{k!}$$

Proof: the monitoring area is $S$, in the monitoring region of arbitrary nodes subordinated to the node distribution probability of $P=A/S$, when the number of nodes of $n$ probability obeys two type distributions is:

$$P(X=k)=Cn^k\lambda^kA^k(n-k)!k!$$

According to the node density formula $\lambda=n/S$ into arbitrary node distribution probability of $P$:

$$P=\lambda A/n$$

Equation (5) into the formula (4):

$$P(X=k)=n!(\lambda A)(1-\lambda A/n)n/(n-k)!k! (n-\lambda A)k$$

When $n\to\infty$, and its limit available:

$$P(X=k)=\lim(n!(\lambda A)(1-\lambda A/n)n/(n-k)!k! (n-\lambda A)k) = e^{-\lambda A}(\lambda A/k)!$$

4. Nonlinear Coverage Control

When the focus of the target node is considered to be the key target [17], it will be covered with multiple sensor nodes, in order to achieve the purpose of the cover and positioned accurately. Each node in the process of cover, for a certain probability to choose their own work nodes, there're a total of five kinds of state covering process can convert each other, constitute the node scheduling strategy. As shown in figure 2.

![Figure 2. Networks Coverage Model](image)

Diagram shows the sensor nodes in the process of monitoring area covering the target node data information obtained through the perception scope, by calculation and forwarded to neighbor nodes or anchor node; At the same time using multiple sensor node to destination node formed by multiple coverage to determine the focus of the target node, the coverage is greater than or equal to 2.

When the target into a cluster head monitoring area, to the neighbor cluster head node sends a packet containing the target information, all the monitoring to the target cluster
are dynamically in the target around to form a group, cluster member nodes only with the cluster node communication, the cluster head and between cluster heads can be mutually communication. Involved in tracking the cluster number depending on the size of the radius of the grid. For example, if the access grid side length equal to the radius of communication node, then a maximum of only four cluster capable of simultaneously monitoring to the target. When at the same time two or more than two cluster head and monitoring to the target, we select these clusters in a cluster head node as a leader node, cluster head first to the neighbor hair to send their and monitoring the distance between the target data information, if the cluster head received a distance closer to the target hair to information, give up campaign to become leader node. Selection criteria for: first, choose from the closest cluster head node; second, if there are two or more than two cluster head node and the target and the distance between the same, residual energy larger the lead node. All the monitoring to the target cluster head node will be sent to a leader node data first, and then by the leading node calculation and data fusion are transmitted to a data center node. As shown in figure 3:

When the mobile target leading away from the node, because of the need to transmit data over long distances to the leader node, or a new cluster head node monitoring to the target, then a leader node is no longer applicable acts as a leader node, fast the election of a new leader node is very necessary. Here we shall, when there is a new cluster head node joins the mobile target tracking, under the leadership of node selection rules, in all involved in tracking the cluster head node selects a distance to a target the nearest cluster head node as its new leader node, data reported by the new leader node is sent to a data center [16].

The sensor node is a round number as the cycle to work. During an initialization phase, the sensor node closed its induction module, update their information and the neighbor node. In the scheduling process to go through five states, respectively, the start state, judge state of competition state, hibernation, the listening state, a five state conversion constitute the sensor node scheduling strategy. First of all, to judge if the node meet the dormancy condition, such as meet into hibernation, or into the competitive status, when entering into competition, start a timer; secondly, when the node competitive success, node to the start state, competition failure node into the listening state; again, in a sense node on success to receive the neighbor node to broadcast news On-duty Message, update its neighbor nodes' information, thus entering the judgment condition; fourth, in the starting state of the node to its neighbor node sends a On-duty Message, which contains the start node only ID identification and location information, and carries on the effective coverage of the work; fifth, in order to save the energy of the node, for accurate monitoring region to effectively cover, the sensor node will turn off unnecessary device to prolong the network life cycle. In practical application process, the sensor node according to the neighbor node's information to dispatch their information, until sure sensor node itself as the start state or resting state so far, as shown in figure 4:
Wireless sensor network node energy consumption most are from to in data processing and communication, contains the main data calculation, data processing and data transmission on three aspects, including data transmission by the consumption of energy is higher, the wireless communication consumption model was studied, its model:

$$E_{Tr}(k,d) = E_{elec} + E_{amp}(k,d)$$

(8)

In order to verify the effectiveness of the algorithm and stability, the experiment from the two aspects of the comparison, the simulation platform is MATLAB7, the simulation region is set to 500m×500m, sensor nodes is 300, sensor node sensing radius is 5m, the initial each node's energy is the same 2J, network bandwidth is 1Mbps, packet size is 100bits, the sampling period is 10s.

The first case: the algorithm and LEACH protocol comparison experiment, validation in the same round number, the network energy consumption contrast conditions, as shown in figure 5:

From the figure 4 can be seen, in the initial moments, two algorithms of the network energy consumption approximately equal; but as time goes on, the algorithm of the network energy consumption less than LEACH protocol of energy consumption, and this algorithm to the subsequent time tends to be stable, in the entire network cover cycle, this algorithm can effectively save the sensor node energy, prolong the network life cycle.

In second cases, using this algorithm with PEAS algorithm in coverage on the comparison experiment, the coverage rate of 99% that is completely covered, the experimental data are in 100 simulation data by extracting the average value, as shown in figure 6:
From seeing the figure 5, as time progresses, two algorithms of coverage has declined. The initial phase, two algorithms of coverage, but in t=1500, PEAS algorithm coverage declined more obvious, the algorithm still maintain higher coverage. In the same node under the effect of this algorithm, coverage was significantly higher than that of PEAS algorithm, to verify the effectiveness of this algorithm.

In order to achieve the scale of network coverage, and thus better evaluate the performance of the model in different sizes, which mainly reflect the minimum number of nodes needs to be deployed in different network coverage, each simulation experiment executed 50 times at average. Curve of node coverage changes is shown in figure 7:

![Figure 6. Different Rounds of the Network Coverage](image)

**Figure 6. Different Rounds of the Network Coverage**

Figure 7 shows the graph of the number of sensor nodes needed to deploy to achieve different node coverage under different network dimensions. The figure shows that, with the expansion of the network, to meet the demand for network coverage, the number of nodes required to be deployed will increase, and the higher the coverage of the network, the number of nodes need to be deployed increases can be obtained from Figure more fast, so that the concern target node can achieve complete coverage.

Experiment: Figure 8 shows a diagram of the number of sensor nodes need to be deployed for the same network size 400 * 400m2 under different node coverage requirement, and compare with the experiments of literature SCCP algorithm, to meet certain demand for network coverage, the number of nodes deployed will be gradually increased as time progresses, and the network coverage will also increase, so that completely coverage is achieved for the same coverage area and different nodes coverage for target area, as shown in figure 8:

![Figure 7. Coverage Rate for Different Coverage Area](image)
6. Conclusion

This paper studies the coverage problem in wireless sensor network, using the node to node state transition mechanism for effective control, giving the Poisson distribution model and reasoning the joint probability density, and verifying the efficiency of coverage, quantifying the node density distribution, optimizing the network resources. Using relationship between the sensor node and the target node, it gives the coverage model of monitoring region network, identifies the sensor node and the target node affiliation, as well as the effects that $K$ heavy coverage puts on the network monitoring region. Using the node state transition mechanism, it constructs the node wheels work system model. Finally through the simulation experiment on the LEACH protocol and PEAS algorithm comparison experiment, in the network energy consumption and network coverage rate of this algorithm, this paper is higher than above two algorithms, achieving the goal of prolonging the network lifetime and improving the quality of network service.

Acknowledgements

This work is supported by the Key Project of Science of Technology Research of Foundation Project of Henan Province Education Department under Grant (No. 2014B520099), and Natural Science and Technology Research of Foundation Project of Henan Province Department of Science under Grant (No. 142102210471).

References


Authors

**Huiling Peng**, she was born in 1980 in Zhoukou city Henan province. In 2007 graduated from Jiangxi University Science & Technology, Master of Science; she is a lecturer in Luoyang institute of Science and technology, Computer and Information Engineering. The main research interest is wireless sensor network and parallel processing.

**Zeyu Sun**, he was born in 1977 in Changchun city, Jilin province, in 2010 graduated from Lanzhou University, Master of Science; Xi’an Jiao tong University study for PhD at present. He is a lecturer in Luoyang institute of technology of computer and information engineering, is also a member of China computer society. The main research interest is in wireless sensor networks, parallel computing and Internet of things.